# Problem A. Explosions

Input file:	standard	input
Output file:	standard	output

Imagine we place some cans of explosives on a long, straight fence. When a can is shot, it will explode. Different types of explosives have different blast radii. Each can contains only one kind of explosive.

When a can explodes, if another can is in the blast radius, then that can will also explode, possibly creating a chain reaction. Each can explodes only once. This process continues until all explosions stop. For each can, suppose that it is the only can shot. How many cans in total will explode?

### Input

There will be several test cases in the input. Each test case will begin with a line with a single integer  $n \ (1 \le n \le 10^5)$  representing the number of cans on that fence. Each of the next n lines will have two integers  $x \ (-10^9 \le x \le 10^9)$  and  $r \ (1 \le r \le 10^9)$ , where x is the location of the can on the fence and r is the blast radius. No two cans will occupy the same location. The input will end with a line with a single 0.

### Output

For each fence, print n integers on a single line separated by single spaces. The *i*-th integer represents the number of cans that will explode if the ith can is the one that is shot. Output no extra spaces, and do not print any blank lines between outputs.

standard input	standard output
3	1 2 1
4 3	1 3 1 1 9 9 1 9 2 2 9 1
-10 9	
-2 3	
12	
2 2	
77	
10 1	
19 3	
23 12	
29 8	
33 1	
35 17	
39 2	
40 1	
46 11	
52 3	
0	

# **Problem B. Flooding Fields**

Input file:	standard	input
Output file:	standard	output

Farmer John has a problem: it's raining, and his pastures are at risk of flooding. Luckily he's invested in a state-of-the-art drain system that ensures that the water level is the same across the farm. He hasn't been as lucky with the terrain. Farmer John's cows can only stand on dry land: if the land becomes wet, any cow on that land drowns. Luckily, cows can move horisontally or vertically one grid sector each hour, giving them a chance to escape the water (the levels of which rise and fall each hour).

Farmer John has divided his field into grid sectors, which he indexes with a row and column. Each grid sector is small enough to only be able to hold one cow. Given a description of Farmer John's field, the starting locations of his cows, and the height of the water at each hour, and assuming that Farmer John's cows are extremely intelligent and prescient, and so can always make the best move, what is the maximum number of Farmer John's cows that could survive?

#### Input

There will be several test cases in the input. Each test case will begin with a line with three integers, n  $(1 \le n \le 100)$ , k  $(0 \le k \le 100)$ , and h  $(1 \le h \le 24)$ , where n represents the size of Farmer John's field (it's  $n \times n$  grid sectors), k is the number of cows in the field, and h is the number of hours he needs to track.

Each of the next n lines will contain n integers  $h_i$  each, which represent the height of each grid sector of Farmer John's field ( $0 \le h_i \le 100$ ). The first row in the input is row 0, and the last is row n - 1. The first column in each row is column 0, and the last is column n - 1.

The following k lines will each contain a pair of integers, r followed by  $c \ (0 \le r, c < n)$ . Each line indicates the grid sector position of one cow at hour 0, where r is the row and c is the column. No two cows will be in the same position. The next h lines will each contain a single integer  $l_j$ , indicating the level of the flood at that hour  $(0 \le l_j \le 100)$ . These lines are given in order: hour 1 first, then hour 2, and so on. Note that the times start at hour 1, and the cows positions are given at hour 0, so the cows have an opportunity to move (or MOOOOve) before the first hour's flood. A grid square is considered to be flooded if its height is not greater, than level of the flood at a given hour. Cows can not move diagonally.

The input will end with a line with three 0s, which should not be proceeded.

### Output

For each test case, output a single integer denoting the maximum possible number of surviving cows. Do not output any spaces, and do not print any blank lines between answers.

standard input	standard output	
3 1 3	1	
2 1 2		
3 1 3		
2 4 2		
1 1		
0		
2		
1		
0 0 0		

# Problem C. Goat Ropes

Input file:	standard	input
Output file:	standard	output

A farmer has n goats. Coincidentally, he also has n fixed posts in a field where he wants the goats to graze. He wants to tie each goat to a post with a length of rope. He wants to give each goat as much leeway as possible – but, goat ropes are notorious for getting tangled, so he cannot allow any goat to be able to wander into another goat's territory. What is the maximum amount of rope he could possibly use?

### Input

There will be multiple test cases in the input. Each test case will begin with an integer  $n \ (2 \le n \le 50)$ , indicating the number of posts in the field. On each of the next n lines will be a pair of integers, x and  $y \ (0 \le x \le 1,000, 0 \le y \le 1,000)$  which indicate the cartesian coordinates (in meters) of that post in the field. No two posts will be in the same position. You may assume that the field is large enough that the goats will never encounter its border. The input will end with a line with a single 0, which shouldn't be processed.

### Output

For each test case, output a single floating point number, which indicates the maximum amount of rope that the farmer could possibly use, in meters. Output this value with precision of 0.01. Output no spaces, and do not output a blank line between answers.

standard input	standard output
2	500.0
250 250	603.55
250 750	
3	
250 250	
500 500	
250 750	
0	

# Problem D. Job Postings

Input file:	standard	input
Output file:	standard	output

Your university has jobs available for students, and the administration needs for you to help them assign students to jobs. The goal is to have students select their desired positions, and then allocate each student to one of the positions so that the maximum satisfaction is achieved.

Each student selects four positions, in the order of desirability. First position is most wanted, next position is next most wanted, if the first position is not available for this student, and so on.

Students have seniority, based their year of study. Third-year students selections should have more weight than first-year students selections.

The administration wants for you to use the following satisfaction matrix:

Job/Position choice:	1st	2nd	3rd	4th
1st year student:	4	3	2	1
2nd year student:	8	7	6	5
3rd year student:	12	11	10	9

Your task is to assign students to positions in a way that maximizes the sum of all students satisfaction according to the above matrix. Each student must get a position, but all positions may not be filled.

#### Input

There will be multiple test cases in the input. Each test case will begin with two integers,  $n \ (4 \le n \le 140)$ and  $m \ (1 \le m \le 70)$ , where n is the number of postings and m is the number of students. Each of the next n lines will contain a single integer  $p \ (1 \le p \le 10)$ , indicating the number of positions available for that job posting. The job postings are listed in order, from job 0 to job n - 1.

Following the job postings will be *m* lines describing the students. Each student line will have five integers:  $y_i, c1_i, c2_i, c3_i, c4_i$ , Where  $y_i$   $(1 \le y_i \le 3)$  is the student's year of study, and  $c1_i, c2_i, c3_i$  and  $c4_i$   $(0 \le c1_i, c2_i, c3_i, c4_i < n, all four unique)$  indicating the student's choice of job postings, in order of preference.

It is guaranteed for every test case that a solution exists where every student can get one of the positions on their choice list.

The input will end with a line with two 0s, which shouldn't be proceeded.

### Output

For each test case, output a single integer, which indicates the maximum satisfaction achievable. Output no spaces, and do not output a blank line between answers.

standard input	standard output
4 4	30
1	36
1	
1	
1	
10123	
20123	
30123	
30123	
4 4	
4	
4	
4	
4	
10123	
20123	
30123	
30123	
0 0	

# Problem E. Overlapping Maps

Input file:	standard	input
Output file:	standard	output

Fred and Sam are traveling together. Both have maps of the area. The maps cover exactly the same territory, and have exactly the same ratio of width to height, but Sam's is at a smaller scale than Fred's, so it's a bit smaller. Fred puts his map on a table. Sam throws his map on top of it. The smaller map is offset and rotated, but it still fits entirely on top of the bigger map. Fred sticks a pin in the smaller map. The pin goes all the way through to the bigger map. Sam is amazed! He says "Wow! Do you realize that the position of that pin represents the same place on BOTH maps?" Fred says "it's really not so amazing. There has to be one such point!"

Given the dimensions of a large map, and the offset, scale and rotation of a smaller map that is entirely on top of the larger map, find the single point that represents the same place on both maps.

### Input

There will be several test cases in the input. Each test case will consist of a single line with six integers w, h, x, y, s, and r. The first two integers w and h (0 < w,  $h \le 1,000$ ) are the width and height of the larger map. The larger map will be on a plane, with the southwest corner at the origin, the northwest corner at (0, h), the southeast corner at (w, 0), and the northeast corner at (w, h).

The next two integers, x and y  $(0 \le x \le w, 0 \le y \le h)$ , represent the (x, y) coordinate on the plane of the southwest corner of the smaller map.

The integer s (0 < s < 100) represents the scale of smaller map as a percentage of the larger map (s = 50 means that the smaller map has half the width and half the height of the larger map). The integer r ( $0 \le r < 360$ ) is the angle, in degrees, of counter-clockwise rotation of the smaller map around its southwest corner (r = 90 means that the southeast corner is rotated to be due north of the southwest corner).

The smaller map is guaranteed to lie completely within the borders of the larger map.

The input will end with a line with six 0s, which shouldn't be proceeded.

### Output

For each test case, output two real numbers, a and b, representing the (a, b) coordinate of the point where both maps represent the same place. Output the numbers to two decimal places of accuracy, with a single space between them. Do not output any extra spaces. Do not put blank lines between answers for different cases.

standard input	standard output
100 100 50 50 25 0	66.667 66.667
100 100 50 50 25 45	45.59 70.53
0 0 0 0 0 0	

# Problem F. 3D-printing

Input file:	standard	input
Output file:	standard	output

3D printing is a technique for manufacturing items from a digital template. The printer lays down layers of a polymer material, building an entire 3D object as a series of flat plates of varying shapes, stacked upon one another. The polymer is initially sticky enough so that the plates printed on top of one another will adhere. After the object dries or cures, the resulting objects can be quite durable.

Consider a 3D printer in which objects to be printed are described as a template, consisting of a combination of several convex polyhedra (i.e., flat-surfaced objects such that a line from one interior point to another interior point never passes outside the volume of the object). Write a program to determine the total volume of polymer required to sculpt an object from a given template.

### Input

There will be several test cases in the input. Each test case will begin with a line with a single integer n  $(1 \le n \le 100)$  representing the number of polyhedra in that template.

The subsequent lines describe the *n* polyhedra. Each polyhedron begins with a line containing an integer f (3 < f < 30), which is the number of faces on the polyhedron. Following that line is a series of lines describing polygons that comprise the faces. Each such line begins with an integer v (3  $\leq v \leq$  24), which is the number of vertices. Following v on the same line will be  $3 \cdot v$  real numbers, representing the v vertices as (x, y, z) coordinates. For example, if v = 3, then the line would be v,  $x_1 y_1$ ,  $z_1$ ,  $x_2 y_2$ ,  $z_2$ ,  $x_3$ ,  $y_3$ ,  $z_3$ .

All coordinates will be between -100 and 100, inclusive. Vertices are presented in sequential order; there will be an edge of the polygon from  $(x_1, y_1, z_1)$  to  $(x_2, y_2, z_2)$ , from  $(x_2, y_2, z_2)$  to  $(x_3, y_3, z_3)$ , and so on. The polygons are closed, so there is an implied edge from the last vertex in a polygon back to the first. All of the vertices of a face will be coplanar. Edges will not cross, and each vertex will lie on exactly two edges. No three (or more) vertices in a polygon will be collinear.

None of the polyhedra in any given test case will overlap. The input will end with a line with a single 0, which shouldn't be proceeded.

## Output

For each template, print a real number on its own line, indicating the volume of polymer required in cubic centimeters. The volume should be printed with a precision of 0.01.

standard input	standard output
2	812.500
6	
4 10 10 0 10 15 0 15 15 0 15 10 0	
4 10 10 0 10 15 0 10 15 20 10 10 20	
4 10 15 0 15 15 0 15 15 20 10 15 20	
4 15 15 0 15 10 0 15 10 20 15 15 20	
4 10 10 0 15 10 0 15 10 20 10 10 20	
4 10 10 20 10 15 20 15 15 20 15 10 20	
6	
4 0 0 0 0 25 0 25 25 0 25 0 0	
4 0 0 0 0 25 0 0 25 0.5 0 0 0.5	
4 0 25 0 25 25 0 25 25 0.5 0 25 0.5	
4 25 25 0 25 0 0 25 0 0.5 25 25 0.5	
4 25 0 0 0 0 0 0 0 0 0.5 25 0 0.5	
4 0 0 0.5 0 25 0.5 25 25 0.5 25 0 0.5	
0	

# Problem G. Roads (Division 1 Only!)

Input file:	standard	input
Output file:	standard	output

Winter is coming, and the citizens of Winterfell are making preparations for the long months ahead. One particular concern is the stability of the roads and bridges; supply lines must stay uninterrupted as the season progresses.

The civil engineers of Winterfell would like to model possible scenarios of roads failing and repairs that need to be made. In their model, each road connects two landmarks in the city, and each road has a certain carrying capacity. Trucks travel from landmark to landmark, and can only travel on sufficiently sturdy roads.

In particular, a supply truck with weight w can travel on a road with capacity c iff  $w \leq c$ . Whether by nature or by accident, the capacity of a road can decrease over time. In addition, repairs can increase the carrying capacity of a road. While roads change, however, supply trucks still need to be able to get from source to destination, and the engineers would like to test whether trucks can still make certain runs between landmarks.

Given a series of changes to the roads and some supply truck runs, help the engineers check whether or not supplies can still be delivered as winter strikes.

### Input

There will be several test cases in the input. Each test case will begin with a line with two integers n,  $m \ (1 \le n \le 1,000, \ 1 \le m \le 100,000)$ , where n is the number of landmarks, and m is the number of roads between them. This will be followed by m lines, each with three integers a, b, and  $c \ (1 \le a, b \le nand1 \le c \le 10^9)$  representing a road between landmarks a and b with carrying capacity c. Roads are numbered  $1, 2, 3, \ldots, m$  in the order that they appear in the input. Next will be a line with a single integer  $e \ (1 \le e \le 10^5)$ , indicating the number of events. This will be followed by e lines, consisting of a capital letter followed by integers:

- Br c: Indicates that road r breaks down. Its carrying capacity decreases to c.  $(1 \le r \le m, 1 \le c < 10^9)$
- R r c: Indicates that road r is repaired. Its carrying capacity increases to c.  $(1 \le r \le m, 1 < c \le 10^9)$
- S a b w: Check whether or not a supply truck with weight w can travel from landmark a to landmark b. (1 ≤ a, b ≤ n, 1 ≤ w ≤ 10<sup>9</sup>).

Only capital letters 'B', 'R' or 'S' will appear. All events occur in the order given in the input. There will be at most 2,000 breakdown/repair events in the input. The input will end with a line with two zeros, which shouldn't be proceeded.

### Output

For each 'S' a b w query, in order, output 1 if the there is a path from a to b that can support a truck of weight w, and 0 if there is not. Output each number on its own line, with no spaces. Do not print any blank lines between outputs.

XIII Open Cup named after E.V. Pankratiev. Stage 5, Grand Prix of America, Division 1, Sunday, April 7, 2013

standard input	standard output
3 4	0
123	1
233	1
2 1 1	0
121	
6	
S 1 2 4	
S 2 3 2	
R 1 4	
S 1 2 4	
B 2 1	
S 2 3 2	
0 0	

# Problem H. Satisfaction Guaranteed (Division 1 Only!)

Input file:	${\tt standard}$	input
Output file:	standard	output

Consider a very simple programming language, with only three types of statements:

```
if <boolean expression> then <statement list> fi
if <boolean expression> then <statement list> else <statement list> fi
checkpoint
```

All keywords are required to consist of all lower case letters. A <statement list> is obviously just a list of one or more statements, and an entire program is a single <statement list>.

A <boolean expression> consists of:

<boolean expression>: A ... Z <boolean expression>: ~<boolean expression> <boolean expression>: <boolean expression>&<boolean expression> <boolean expression>: <boolean expression>|<boolean expression> <boolean expression>: (<boolean expression>)

I.e. as variables are used single capital letters, as operators — unary ' ' (NOT), binary '&' (AND), binary '|' (OR) with precedence: NOT > AND > OR. Parentheses may be used; no spaces are allowed in expression.

Given a syntactically correct program in this simple language, find, what values must the boolean variables hold in order to satisfy each of the checkpoints?

#### Input

Input will be a single syntactically correct program in this simple language. Keywords are guaranteed to be in all lower case, and boolean variables are guaranteed to each be a single upper case letter. White space (space, tab or newline) is guaranteed to separate keywords, and surround expressions. Expressions will not contain whitespace.

Every <statement list> will contain at least one statement. The input program will not use more than 20 of the available variables, and will not contain more than 5,000 statements. No <boolean expression> will be longer than 128 characters.

### Output

For each checkpoint, in the order they appear, output a single line, consisting of '>' followed by either a list of variables, or the word "unreachable". If the checkpoint is reachable, output a list of variables, in alphabetical order, with an upper case letter if it must be true, or a lower case letter if it must be false to reach the checkpoint. Omit the variable if it can be either. If the checkpoint is not reachable, then output the word "unreachable", entirely in lower case. Do not print any spaces, and do not print any blank lines between lines of output.

standard input	standard output
if A then	>A
checkpoint	>unreachable
if ~A then	>a
checkpoint	>
fi	>
else	>aB
checkpoint	
fi	
if (A&B) (~A&~B) then	
checkpoint	
fi	
if A ~A then checkpoint fi	
if B then	
if ~A then checkpoint fi	
fi	

# **Problem I. Trading**

Input file:	standard	input
Output file:	standard	output

A brokerage firm is interested in detecting automatic trading. They believe that a particular algorithm repeats itself; that is, it makes the same sequence of trades at a later time.

The firm has identified a set of 26 key stocks that they believe are likely to be traded in concert, and they've encoded a series of trades as a string of letters: the letter itself indicates the stock, upper case indicates a buy, lower case indicates a sell. They want you to write a program to determine, for any two starting points, the longest sequence of identical trades from those two starting points, starting from and including those starting points as the first trade in the sequence.

### Input

There will be several test cases in the input. Each test case will start with a string s on the first line, consisting solely of upper case and lower case letters  $(1 \le length(s) \le 10^5)$ . On the next line will be an integer q  $(1 \le q \le 10^5)$ , indicating the number of queries. The following q lines each describe a query with two integers, i and j  $(0 \le i < j < length(s))$ , which represent two zero-based positions in the string. The input will end with a line containing only an asterisk ('\*').

### Output

For each query, output a single integer, indicating the length of the longest sequence of trades starting at i which is identical to the sequence of trades starting at j. Output no spaces. Do not print any blank lines between lines of output.

standard input	standard output
ABABABcABABAbAbab	4
3	0
0 2	5
1 6	3
0 7	4
SheSellsSeashellsByTheSeaShore	1
4	0
8 22	
1 20	
8 25	
0 1	
*	

## Problem J. Uniform Subtrees

Input file:	standard input
Output file:	standard output

Define a *uniform tree* as one in which all of the nodes at a given level (i.e. distance from the root) have the same degree (i.e. number of children). Since all of the nodes at a given level have the same number of children, a uniform tree can be represented as simply a list of integers, indicating the number of children at each level. For example, the list [2 3 5 0] represents a tree where the root has 2 children, each child of the root has 3 children, each grandchild has 5 children, and each great-grandchild has no children, and is therefore a leaf. For the purposes of this problem, redefine *subtree* as a connected subgraph of a tree that includes the tree's root. This is a bit different than the typical definition of subtree.

Given a description of a tree, find all of the unique *uniform subtrees* of that tree.

#### Input

There will be several test cases in the input. Each test case will will consist of a single tree with at least one node, represented as a single string on one line. The string will be a sequence of matched opening and closing parentheses. Each matched pair represents a node, and the string between represents its children. There will not be more than 4,000 nodes in the tree. There will be no whitespace, or any other characters, in the string. The input will end with a line with a single 0.

### Output

For each test case, output every unique uniform subtree of the given tree as a list of integers, one subtree (and thus one list) per line. Print a single space between integers, and no spaces anywhere else. Do not print any blank lines between lists, or between test cases. Print the lists for a given test case sorted by the first element, then the second, then the third, and so on.

standard input	standard output
(((()))(()(()))))	0
(())	1 0
0	1 1 0
	1 1 1 0
	1 1 2 0
	1 2 0
	1 3 0
	2 0
	2 1 0
	2 1 1 0
	0
	1 0

# Problem K. Unreal Estate

Input file:	standard	input
Output file:	standard	output

A dishonest landowner is selling off plots of land. He's selling it in large, rectangular plots, but many of the plots overlap, so he's actually selling the same land multiple times! It's not real estate, it's unreal estate!

Given a description of the possibly overlapping rectangular plots of land that the dishonest landowner has sold, determine the total actual area of land covered by them.

#### Input

There will be several test cases in the input. Each test case will begin with a line with a single integer n  $(0 < n \le 5,000)$ , indicating the number of plots of land sold. The next n lines will each have a description of a rectangular plot of land, consisting of four real numbers:  $x_1, y_1, x_2, y_2$ , where  $(x_1, y_1)$  is the southwest corner, and  $(x_2, y_2)$  is the northeast corner  $(-1,000 \le x1 < x2 \le 1,000, -1,000 \le y1 < y2 \le 1,000)$ . Every plot will have an area of at least 1. It is guaranteed that  $100 \cdot x_i$  and  $100 \cdot y_i$  are integers. The input will end with a line with a single 0.

### Output

For each test case, output a single real number, which represents the total actual area covered by all of the rectangular plots of land. Output this number with precision 0.01. Do not print any spaces. Do not print any blank lines between outputs.

standard input	standard output
2	10000.00
0 0 100 100	50000.00
30 30 60 60	
2	
0 100 300 200	
100 0 200 300	
0	

# Problem L. Grid Game (Division 2 Only!)

Input file:	standard	input
Output file:	standard	output

A grid game appears on kids' placemats at many restaurants. The game board comprises a rectangular grid of  $M\times N$  dots .

Two players, referred to as A and B, take turns connecting two adjacent dots in a vertical or horizontal direction. When a player draws a line that closes a unit square (or "box"), then he claims a point for that box. If the line closes several boxes, player claims a point for each of them. The game ends when all boxes have been closed and the winner is the player with the most points. A tie is possible if the number of boxes is even.

The lines drawn by each player in a given game can be recorded as a sequences of moves, each move recorded as a number followed by a letter. First, number the dots row-by-row, starting at 0 for the upper-left dot, 1 for the dot right to 0, M - 1 for rightmost dot in top row, M for the dot down to 0 etc.

Then, specify a move by giving the starting dot number and a direction ('R' — right, 'D — down). For example, "0R" connects the two dots at the left end of the top row of dots and "0D" connects the two dots at the top end of the first column.

Given a full record of the game, determine grid size and game result.

#### Input

The first line of input contains a positive integer T ( $1 \le T \le 200$ ) giving the number of lines that follow. Each of the lines after the first gives the record of a game. Assume Player A always moves first. All moves are valid. The maximum grid size is  $50 \times 50$  dots.

#### Output

The output for each line is the number of the game, starting with 1, followed by the size of the grid "<number of columns>X<number of rows>", followed by the result, one of "A WINS", "B WINS", or "TIE". Refer to sample output for clarification.

standard input	standard output	
4	1 2X2 B WINS	
OR1D2R0D	2 3X3 TIE	
0R1D4R4D7R6R2D3D5D3R1R0D	3 3X2 A WINS	
OR1R0D2D3R4R1D	4 4X2 B WINS	
3D0D2R4R2D1D6R0R1R5R		

# Problem M. McDonalds Search (Division 2 Only!)

Input file:	standard	input
Output file:	standard	output

Traveling from Moscow, Idaho to St.Petersburg, Florida, farmer John decided it would be fun to try and visit all the MCDonald's along the way. Of course, "along the way" could be interpreted many ways. So for the purpose of the programming contest, we shall define it as " not more than 2 miles of the interstate exit." Your job is to write a program that will give John a list of the McDonald's that meet this criteria.

### Input

The location of all the McDonald's along the way. Each McDonald's will be on a line by itself in the format:

Name of exit, Distance of exit from Moscow, Distance of McDonald's from exit

Distance of exit from Moscow will be an integer, less or equal to 500. Distance of McDonald's from exit will be a floating point number with at most 2 digits of precision.

There will be maximum 3000 McDonald's locations. Input is terminated by the string "END" (quotes for clarity). There will be no leading or trailing spaces in any of the lines in the input data.

### Output

A list, one per line, of all the McDonald's which meet the criteria, in the order in which we will encounter them on John's journey to St.Petersburg, without backtracking on the interstate. If multiple McDonald's are at the same exit, they should be listed in order of increasing distance from the exit. There will be no two McDonald's at the same exit with the same distance from the exit.

standard input	standard output
South Bridge Road,40,1.5	Green Street, Exit 25
River Blvd,25,4.2	South Bridge Road, Exit 40
Green Street,25,1.0	
Privet Drive,25,50	
Yellow Brick Road,150,4	
END	